

$$S_L = \{(x_i, y_i) : x_{ij} \leq t\}, S_R = \{(x_i, y_i) : x_{ij} > t\}$$

$$(j^*, t^*) = \underset{t}{\operatorname{argmin}} |S_L| l(S_L) + |S_R| l(S_R)$$

$\hat{p}_c$  = emp frac of class  $c$  in a set

Why?  $l(S) = \sum_c \hat{p}_c (1 - \hat{p}_c) \leftarrow \text{Gini}$

Feat 1	Feat 2	Label
0	0	0
1	0	1
1	0	0
1	1	1
1	0	0
1	1	1
1	0	0
1	1	1
1	1	0
1	1	1

Wrong way

$$\text{Feat 1: } 0 + \frac{4}{9} \left( \frac{5}{9} \right) = 0.247$$

$$\text{Feat 2: } \frac{4}{5} \left( \frac{1}{5} \right) + \frac{4}{5} \left( \frac{1}{5} \right) = 0.32$$

0.16      0.16

Right way

$$\text{Feat 1: } 1 - 0 + 9 \cdot \frac{4}{9} \left( \frac{5}{9} \right) = 1.79$$

$$\text{Feat 2: } 5 \cdot \frac{4}{5} \cdot \frac{1}{5} + 5 \cdot \frac{4}{5} \cdot \frac{1}{5} = 1.6$$